



Fearless optimization and Formal verification of post-quantum cryptographic code at AWS

Rod Chapman (he/him/his)

AWS Cryptography

The big ideas...

Hybrid Verification

and

Fearless Optimization



But first ... some data...

MLKEM Number-Theoretic Transform (NTT) running on Graviton2 (EC2 c6g instance) performance in clock cycles. Lower is better.

Code language/version	Cycles
PQCrystals/Kyber reference C code	3481
Rod's very naïve first formally verified version	9110
Rod's best formally verified and optimized version	1239
Hand-written, formally verified AArch64 assembly ("Clean" version)	language 900
AArch64 assembly, auto-super-optimized (also formally verified)	808



The problem...

Cryptographic code is foundational for AWS

Extraordinarily high bar for verification
Functional correctness
Performance (at AWS Scale, this really matters...)
Freedom from known side-channel attacks
Plus...
Longevity



Agility

Crypto Library Layers...

TLS, Quic protocols,
AWS Services, AWS SDKs, Upstream Open-Source Projects, Customer
code... everything else...

Bindings to Rust, Java etc.

AWS-LC

Full cryptographic library. FIPS Validated.

New PQC algorithms.

Hand-written assembly language for x86_64 and AArch64.





Crypto Library Layers...

TLS, Quic protocols, AWS Services, AWS SDKs, Upstream Open-Source Projects, Customer code... everything else... Bindings to Rust, Java etc. **AWS-LC** mlkem-native mldsa-native s2n-bignum

Each "Blob" is a standalone repository on GitHub, permissively licensed, and may be re-used by you.

Back to the plot...The big ideas...

Hybrid Verification

and

Fearless Optimization



Hybrid Verification? Eh?

Mix dynamic and static verification

Dynamic – aka "testing" – using KATs, fuzz testing, runtime assertion checking, Valgrind (including constant-time checking) etc. etc.

Static – aka "Formal Verification" or "Proof" of program correctness properties.



Hybrid Verification? Eh?

Big idea 2:

Modulate the *depth* of Static Verification to get the most bangfor-the-buck. Trade depth for scale pragmatically.



The SV "Depth Gauge"

Bronze: basic "linting" for dumb bugs plus all the dynamic verification.

Silver: Bronze + proof of memory-safety and type-safety.

Gold: Silver + Proof of functional correctness with respect to a formal specification (e.g maths, Cryptol)



Why does this matter?

Fully static verification of type-safety offers the most bang-for-thebuck.

Can be *fully automated* using languages that offer contracts and/or an expressive type system.

Good news: it takes a bit of work, but safety-critical industry have been doing this for years. The tech is well understood.



The big ideas...

Hybrid Verification

and

Fearless Optimization



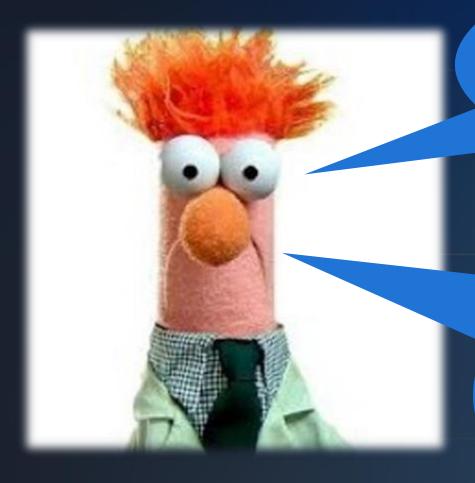
Why does this work?



Well-typed programs cannot "go wrong"...
Robin Milner



Why does this work?



Proven type-safe programs run really fast as well...

Contemporary high-level language compilers are incredibly reliable if you only compile type-safe programs.



"Fearless optimization..." ...Supported by Proof

Reference code.
Correct but not fast enough.

Terminate when returns diminish...

Optimize

Reprove



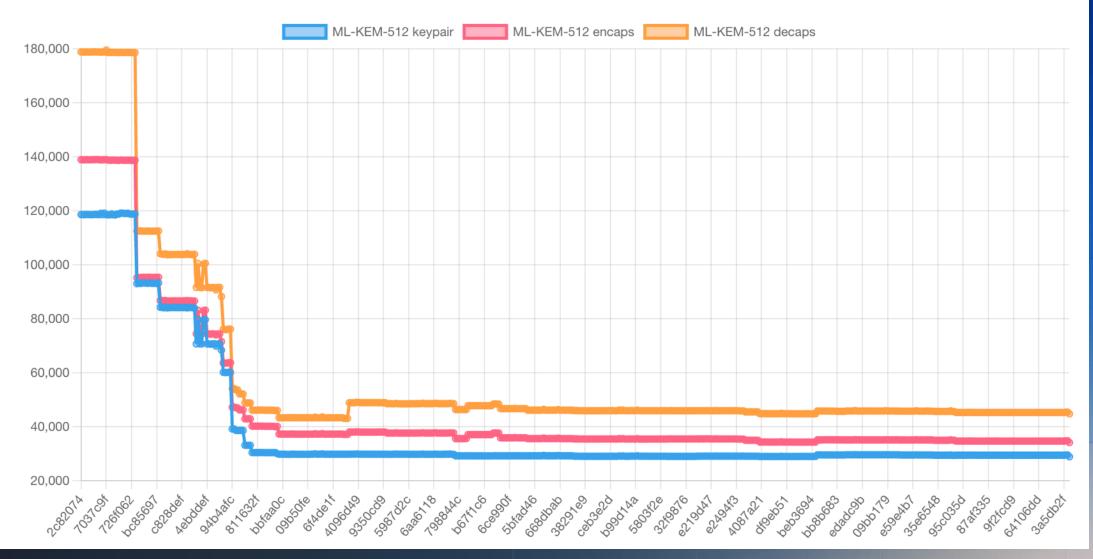


"Fearless optimization..."

...Driven by Proof



Graviton2





An open-source implementation of FIPS-203 (MLKEM).

Already integrated with

AWS-LC

Linux Foundation's LibOQS



Designed to deliver strong performance and assurance for server-class hardware (e.g. AWS Data Centres).

NOT designed for high-threat embedded applications (code exhibits cryptographic constant-time, but not designed to resist power-analysis...)



"Front end" – portable C code.

"Back-end" – implements time- and security-critical functions. There are 4 of these...

- 1. Intel x86_64 AVX2 assembly language
- 2. AArch64 NEON assembly language
- 3. RISC-V RV64imv assembly language
- 4. C (for every other machine)



Static Verification status:

All C code proven type-safe using contracts and CBMC tool in "auto-active" style.

AArch64 – proven functionally correct using HOL-Light (15 functions).

Intel AVX2 – will be proved in HOL-Light. Work-in-progress.

RISC-V RV64imv – not yet (not an AWS-led effort anyway...)



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How did this get done?



Optimizing MLKEM in C...

There are many "standard tricks"

- Montgomery representation and multiplication of polynomial coefficients.
- Barrett reduction
- "Layer merging" of the NTT and Inverse NTT
- Deferred modular reduction
- Caching intermediate results in polynomial multiplication

All verified and defended by continuous proof of typesafety in CI.



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Introducing...

The Super (Lazy) Optimization of Tricky Handwritten assembly



aka "SLOTHY"



SLOTHY?

Inputs

- Plain "clean" human-written assembly language.
- Description of target machine micro-architecture.
 (e.g. number and capabilities of each pipeline, instruction latencies etc.)

Output

Equivalent, but faster code.

Limitation

Only works for AArch64 code at the moment.



How does SLOTHY work?

- Register re-allocation. Use more registers to remove apparent data-flow dependencies.
- 2. Re-order instructions to use more execution pipelines, more of the time.
- 3. Unwind and re-structure inner loops.

(Under the hood – constraint solving)



SLOTHY results

SLOTHY has been used on hand-written code in AWS-LC and s2n-bignum libraries, including RSA, Elliptic-Curves, the AArch64 back-ends for MLKEM and MLDSA.

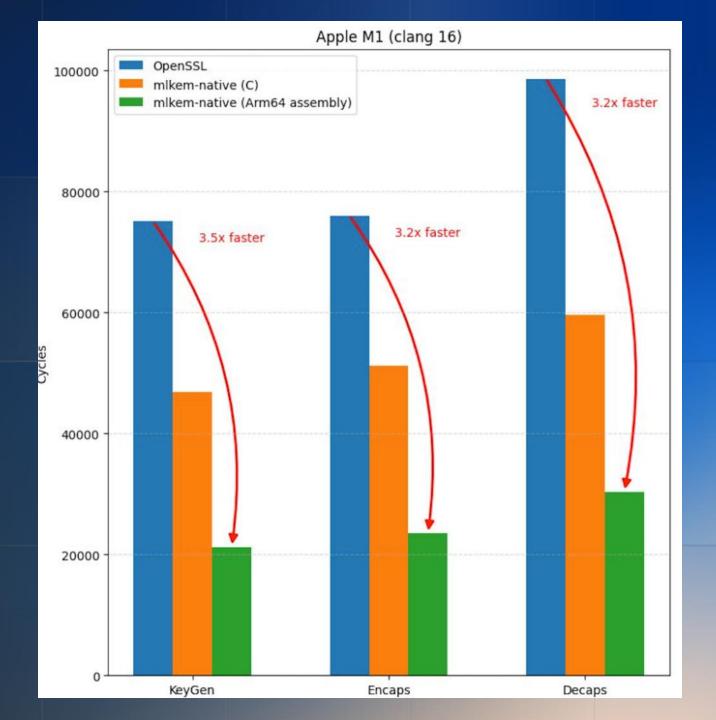
Noticeable performance improvement on Graviton-2 over original hand-written code.

Seems to work well for most AArch64 implementations, including Cortex-Axx, neoverse, Apple M1 etc.



Putting it all together

mlkem-native vs
OpenSSL 3.5





Resources...

s2n-bignum: https://github.com/awslabs/s2n-bignum

mlkem-native: https://github.com/pq-code-package/mlkem-native

mldsa-native: https://github.com/pq-code-package/mldsa-native

AWS-LC: https://github.com/aws/aws-lc

SLOTHY: https://github.com/slothy-optimizer/slothy



Questions...

rodchap@amazon.co.uk

